

# 20.330 / 6.023 / 2.793 Fields, Forces and Flows in Biological Systems

Instructors: Jongyoon “Jay” Han and Scott Manalis

## TOPICS

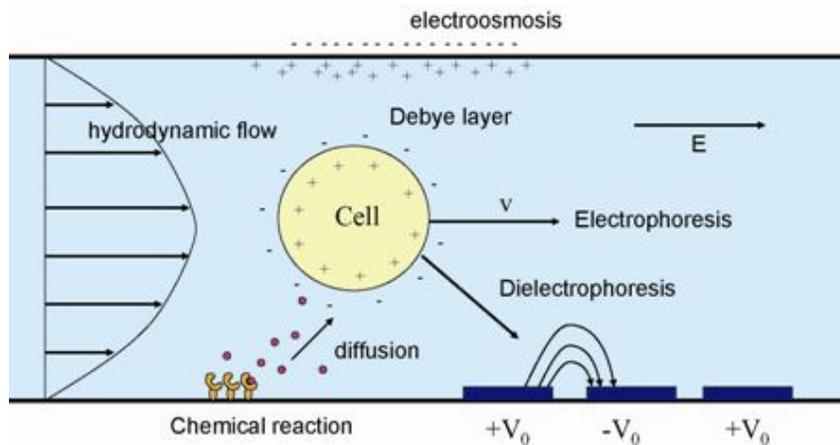
Introduction to electric fields  
 Maxwell's equations  
 Introduction to fluid flows  
 Transport phenomena in biological systems  
 Electro-quasistatics  
 Electrokinetics  
 Electrophoresis  
 Van der Waals and other forces



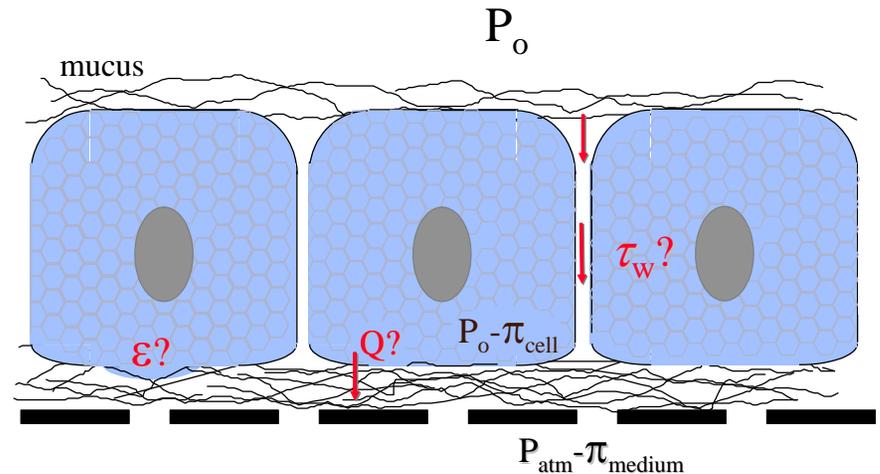
Photo courtesy of 'elbisreverri'.

<http://www.flickr.com/photos/elbisreverri/53226345/>

## Relevant forces in biological systems and nanoscale



Fields/ forces/ flows/ transport in bio-microsystems (bioMEMS)



Transport in living cell and tissue systems

Monday	Tuesday	Wednesday	Thursday	Friday
Registration Day 2/5 L1	No class 2/6	Intro (JS) Fluid 1 (J) 2/7 L1	Tutorial: Curl and Divergence 2/8	Fluid 2 (J) 2/9 L2
Fluid 3 (J) 2/12 L3	Office hours 2/13	Fluid 4 (J) 2/14 L4	Office hours 2/15	<b>HW 1 due</b> 2/16 L5 Fluid 5 (J)
Presidents' Day 2/19	(Monday) Fluid 6 (S) 2/20 L6	Fluid 7 (S) 2/21 L7	Office hours 2/22	<b>HW 2 due</b> 2/23 L8 Fluid 8 (S)
Fluid 9 (S) 2/26 L9	Office hours 2/27	Fluid 10 (S) 2/28 L10	Office hours 3/1	<b>HW 3 due</b> 3/2 L11 Field 1 (J)
Field 2 (J) 3/5 L12	Special office hours for Quiz 1 3/6	Quiz 1 (in class) HW 1-3, L1~10 3/7	Office hours 3/8	(Add Date) 3/9 L13 Field 3 (J)
Field 4 (J) 3/12 L14	Office hours 3/13	Field 5 (J) 3/14 L15	Tutorial: Using the FEMLAB 3/15	<b>HW 4 due</b> 3/16 L16 Field 6 (J)
Field 7 (J) 3/19 L17	Office hours 3/20	Field 8 (J) 3/21 L18	Office hours 3/22	<b>HW 5 due</b> 3/23 L19 Field 9 (J)
Spring Break 3/26 3/27 3/28 3/29 3/30				
Transport 1 (S) 4/2 L20	Office hours 4/3	Transport 2 (S) 4/4 L21	Tutorial / Office hours 4/5	<b>HW 6 due</b> 4/6 L22 Transport 3 (S)
Transport 4 (S) 4/9 L23	Office hours 4/10	Transport 5 (S) 4/11 L24	Tutorial / Office hours 4/12	<b>HW 7 due</b> 4/13 L25 Transport 6 (S)
Patriots' Day 4/16	(Special office hours for Quiz 2) 4/17	Quiz 2 (in class) HW 4-7, L11~24 4/18	Tutorial/ Office hours 4/19	4/20 L26 Transport 7 (S)
Transport 8 (S) 4/23 L27	Office hours 4/24	Transport 9 (S) 4/25 L28	(Drop date) 4/26 Tutorial / Office hours	<b>HW 8 due</b> 4/27 L29 EK 1 (S)
EK 2 (S) 4/30 L30	Office hours 5/1	EK 3 (S) 5/2 L31	Tutorial / Office hours 5/3	<b>HW 9 due</b> 5/4 L32 EK 4 (J)
EK 5 (J) 5/7 L33	Office hours 5/8	EK 6 (J) 5/9 L34	Tutorial / Office hours 5/10	<b>HW 10 due</b> 5/11 L35 EK 7 (J)
EK 8 (J) 5/14 L36	Office hours 5/15	EK 9 (J) 5/16 L37	Office hours 5/17	5/18 Study Period
5/21 5/22 5/23 5/24 5/25 Final Exam Period (3 hour long, comprehensive)				

## Textbooks

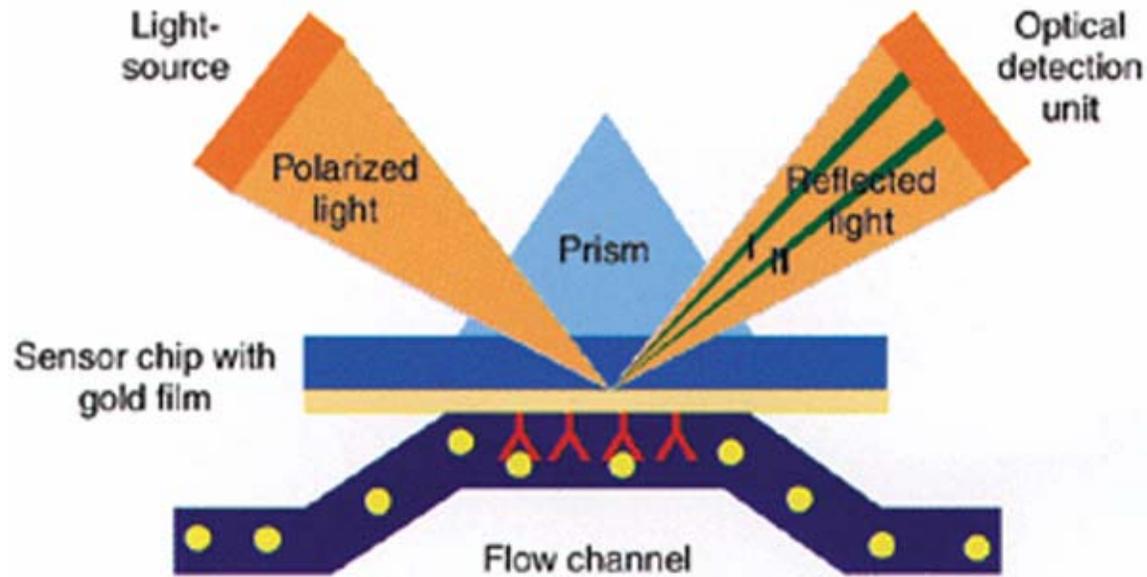
- **Truskey, Yuan and Katz “Transport Phenomena in Biological Systems”** Prentice Hall (REQUIRED)
- Haus and Melcher **“Electromagnetic Fields and Energy”**  
Content available on the web for free  
([http://web.mit.edu/6.013\\_book/www/](http://web.mit.edu/6.013_book/www/))
- **“Physicochemical Hydrodynamics, An Introduction”**,  
by Ronald F. Probstein. (e-reserve)
- **“Electromechanics of Particles”** by Thomas B. Jones,  
Cambridge University Press (e-reserve)
- Other references:
  - Bird/Stewart/Lightfoot, “Transport Phenomena” Wiley
  - Tom Weiss “Cellular Biophysics” Volume 1. Transport, MIT press.
  - “AC Electrokinetics: colloids and nanoparticles”, by Morgan and Green, Research Studies Press.
  - “Principles of Colloid and Surface Chemistry”, by Hiemenz and Rajagopalan, Marcel Dekker.
  - “Molecular Driving Forces”, by Ken Dill and Sarina Bromberg, Garland Science

# How precise can a cell measure the concentration of its environment?

## E. Coli trajectory

Images removed due to copyright restrictions. See Figs. 1 & 3.

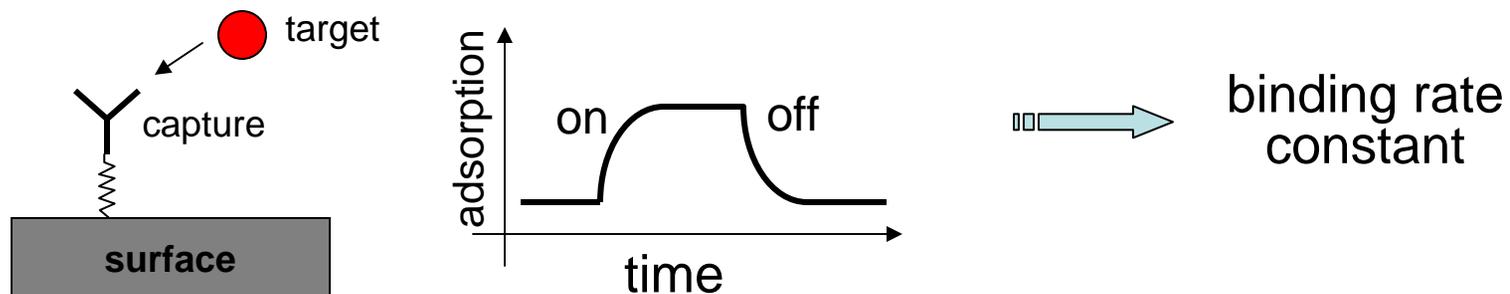
# Measuring binding kinetics



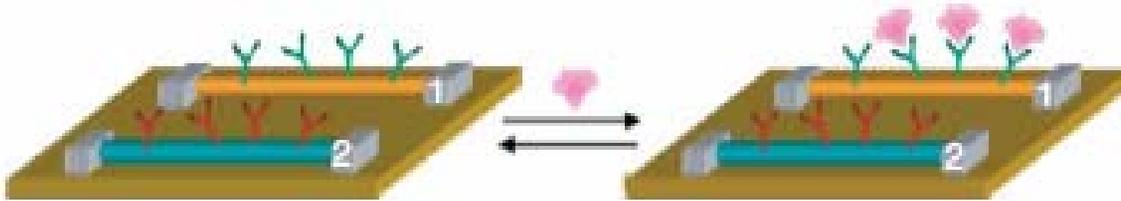
Surface Plasmon Resonance (*Biacore*)

Courtesy of Biacore. Used with permission.

Label-free enables direct readout of  $K_{on}$  and  $K_{off}$



# Detecting biomolecules on the nanoscale



*Nat. Biotech.* 23 (2005)

Courtesy of Dr. Charles M. Lieber. Used with permission.

Source: Fig. 1b in Zheng, G., et al. "Multiplexed electrical detection of cancer markers with nanowire sensor arrays." *Nat Biotech* 23 (2005): 1294-1301.

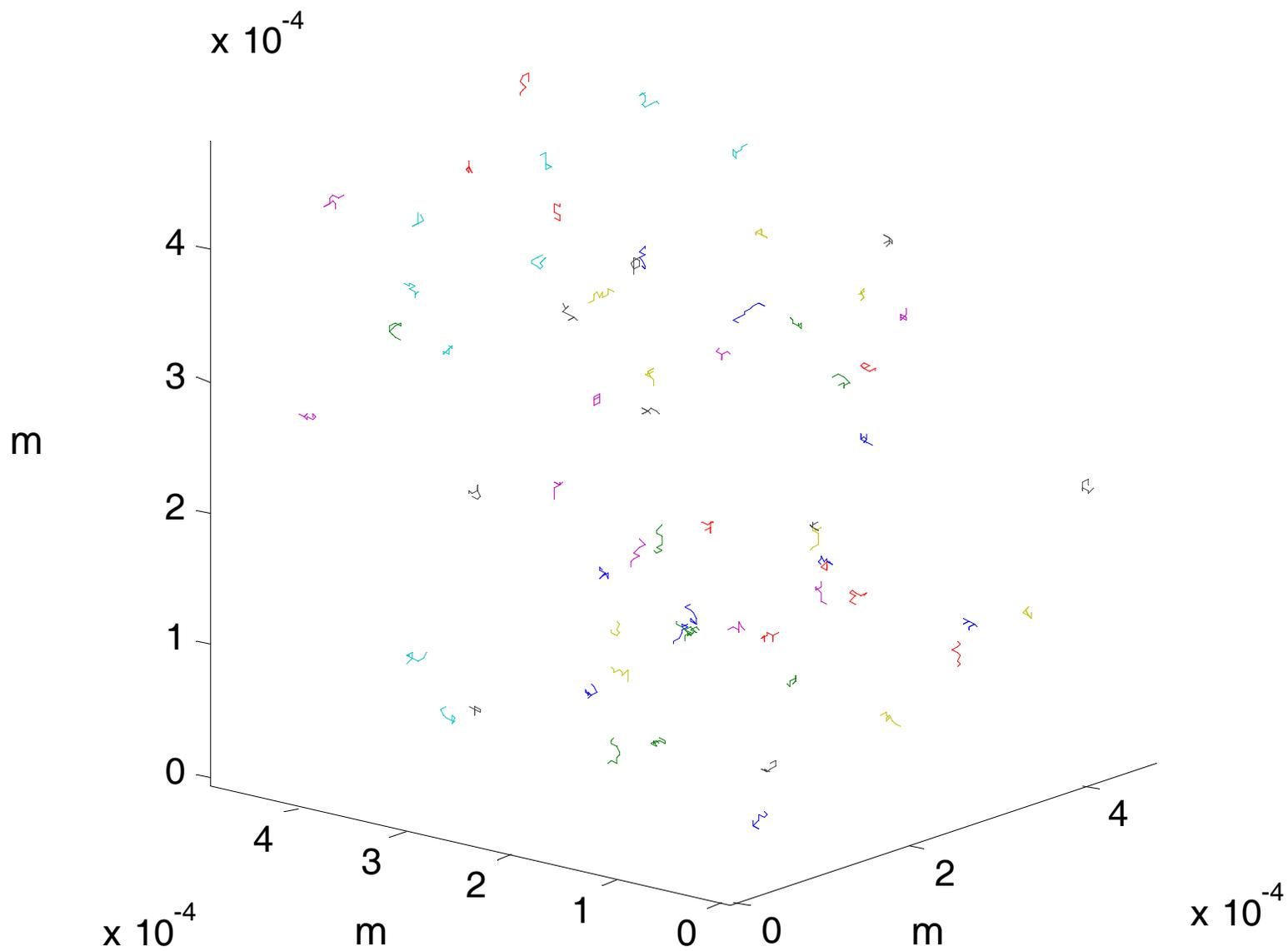
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*J. Am. Chem. Soc.* 128 (2006)

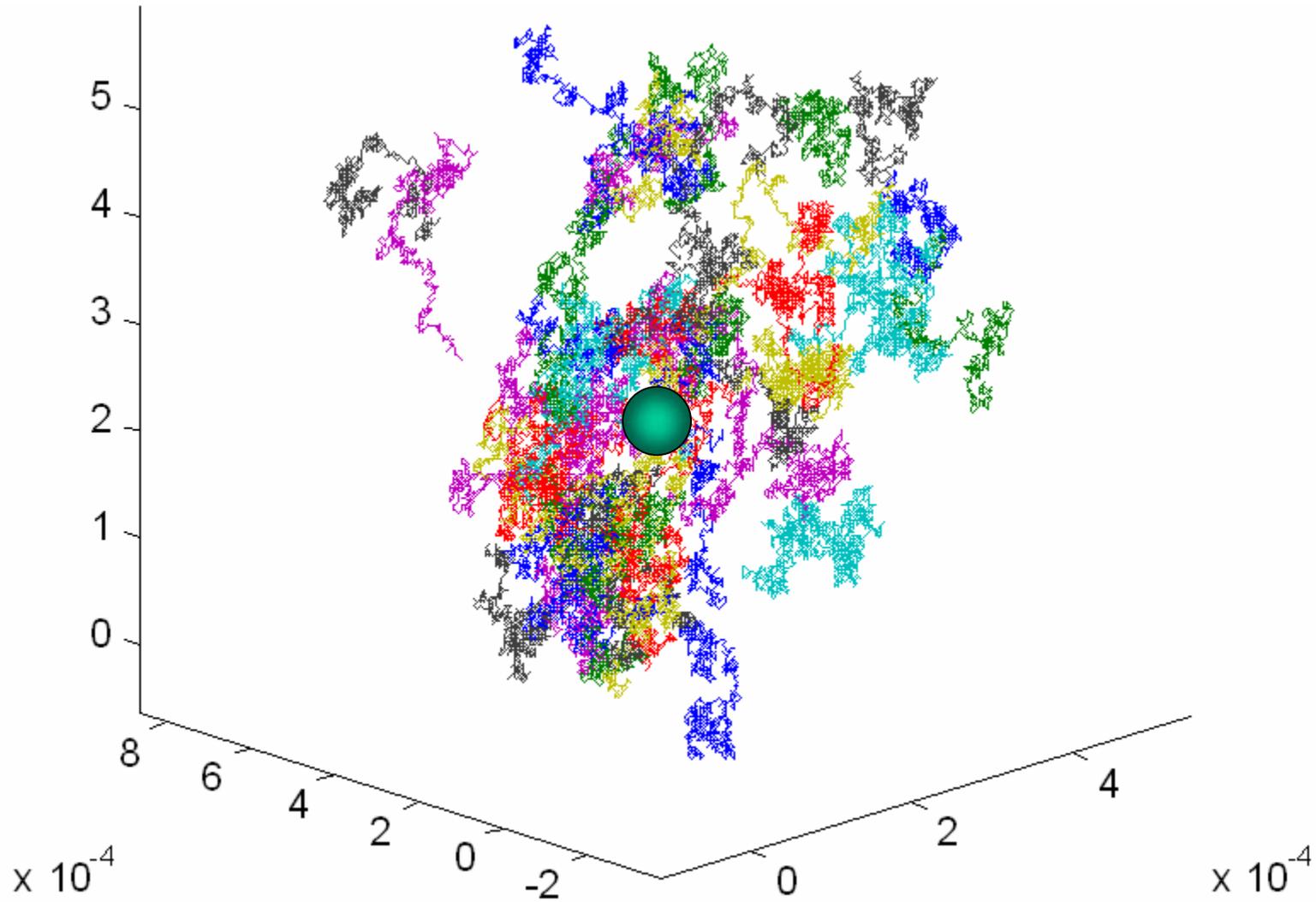
Figure removed due to copyright restrictions.

*Nature* 445 (2007)

# 64 oligos at 1 femtomolar concentration



**...after 10 seconds**



**How often do molecules bind to sphere?**

Proteins : **3D structure** with  
complex charge distribution

Human Serum Albumin

Figure removed due to copyright restrictions.

**Sugio, S., Kashima, A.,  
Mochizuki, S., Noda, M.,  
Kobayashi, K. *Protein Eng.* 12  
*pp.* 439 (1999)**

DNA (SDS-proteins) :  
**Linear polymer** with  
uniform charge density

DNA

Figure removed due to copyright restrictions.

**Brown, T., Leonard, G. A., Booth,  
E. D., Chambers, J, *J Mol Biol*  
*207 pp.* 455 (1989)**

# Migratory birds uses magnets for positioning

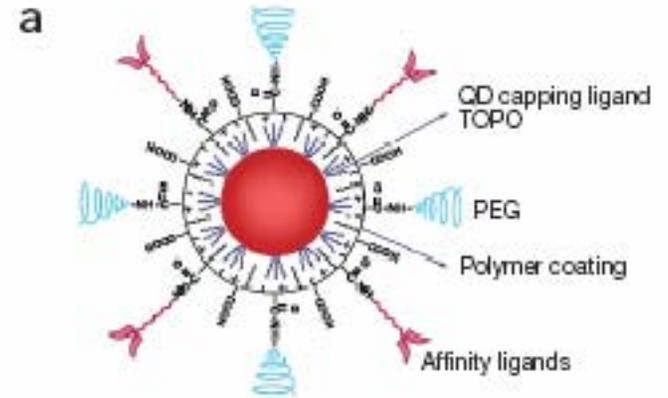
Image removed due to copyright restrictions.

Figure 1 in Mora, Cordula V. "Magnetoreception and its Trigeminal Mediation in the Homing Pigeon." *Nature* 432 (2004): 508-511.

# In vivo cancer targeting and imaging with semiconductor quantum dots

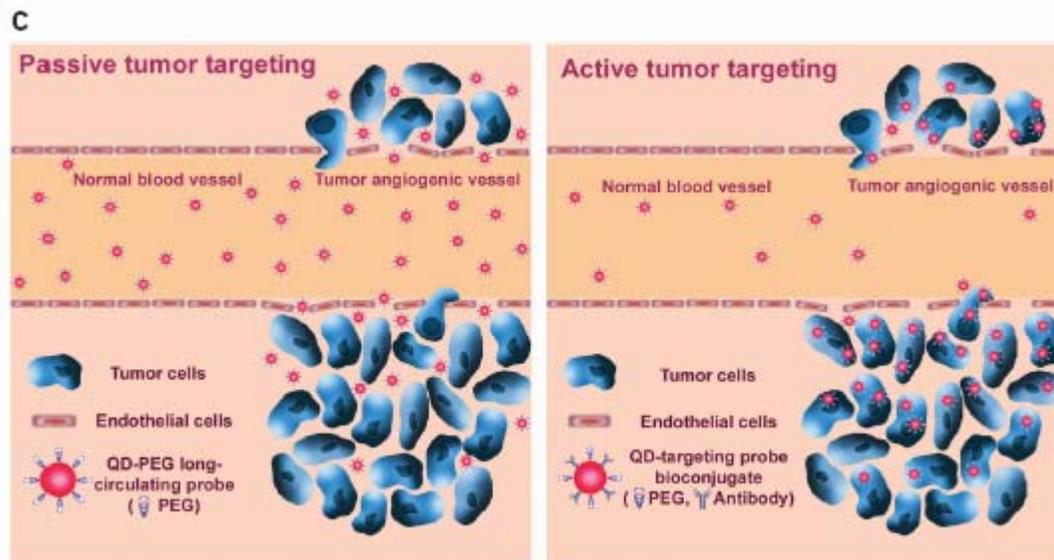
Xiaohu Gao,<sup>1</sup> Yuanyuan Cui,<sup>2</sup> Richard M Levenson,<sup>3</sup> Leland W K Chung<sup>2</sup> & Shuming Nie<sup>1</sup>

We describe the development of multifunctional nanoparticle probes based on semiconductor quantum dots (QDs) for cancer targeting and imaging in living animals. The structural design involves encapsulating luminescent QDs with an ABC triblock copolymer and linking this amphiphilic polymer to tumor-targeting ligands and drug-delivery functionalities. *In vivo* targeting studies in prostate cancer growing in nude mice indicate that the QD probes accumulate at tumors both by the enhanced permeability and retention (EPR) effect and by antibody binding to cancer-specific cell surface biomarkers. Using both subcutaneous injection of QD-tagged cancer cells and systemic injection of multifunctional QD probes, we have achieved sensitive and multicolor fluorescence imaging of cancer cells under *in vivo* conditions. We have also integrated a whole-body macro-illumination system with wide-field spectral imaging for efficient background removal and precise delineation of weak spectral signatures. These results open new possibilities for ultrasensitive and multiplexed imaging of molecular targets *in vivo*.

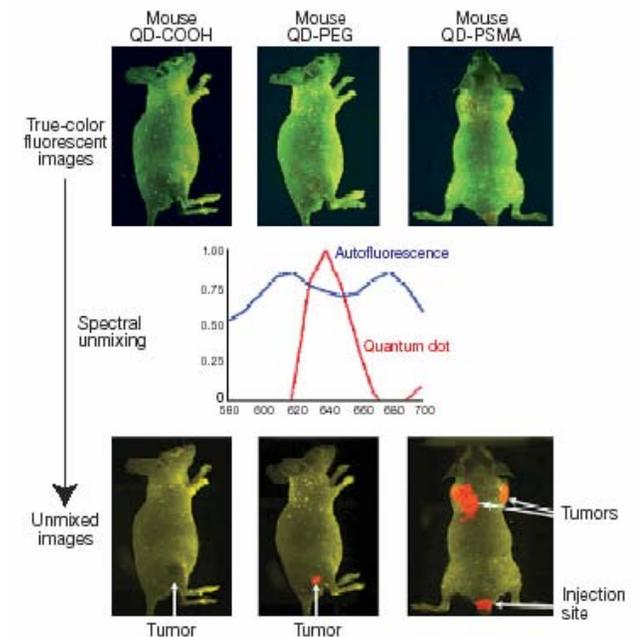


Courtesy of Leland W. K. Chung. Used with permission.

Gao, Cui, Levenson, Chung and Nie, Nature Biotechnology **22**, 969 (2004)



Courtesy of Leland W. K. Chung. Used with permission.



Courtesy of Leland W. K. Chung. Used with permission.

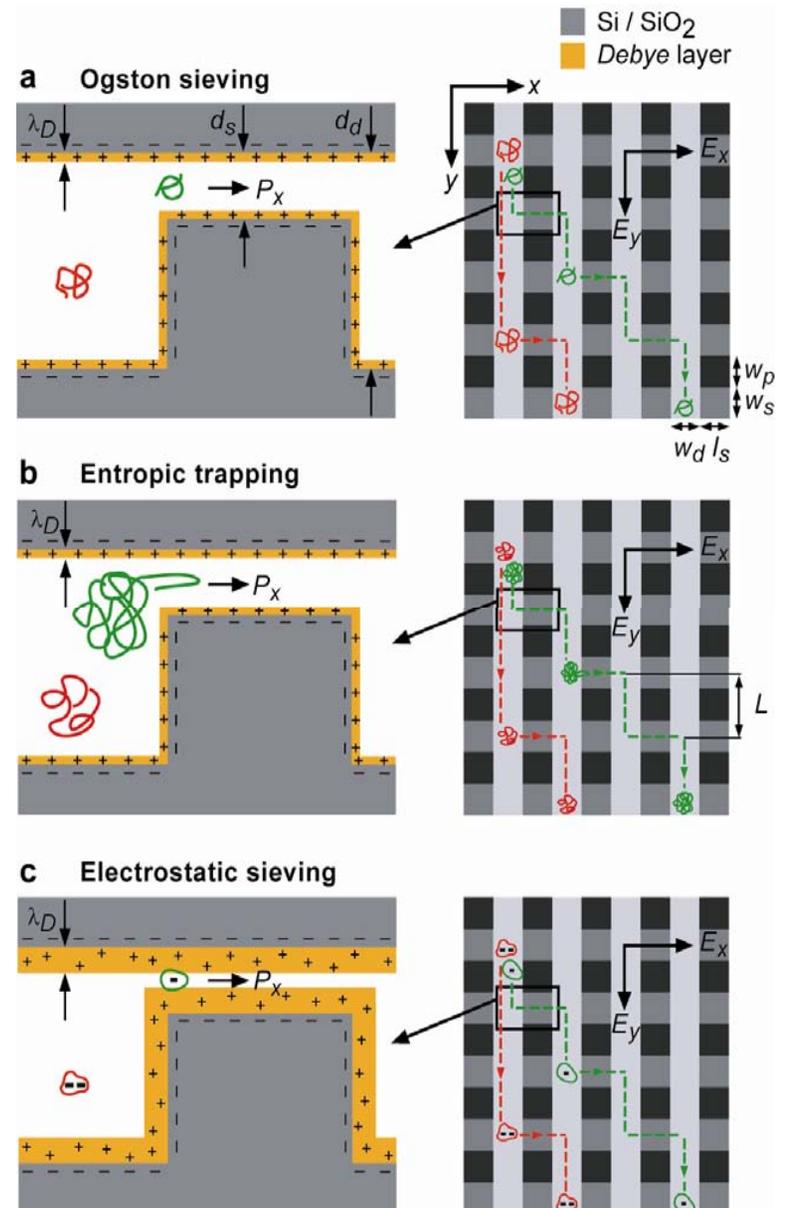
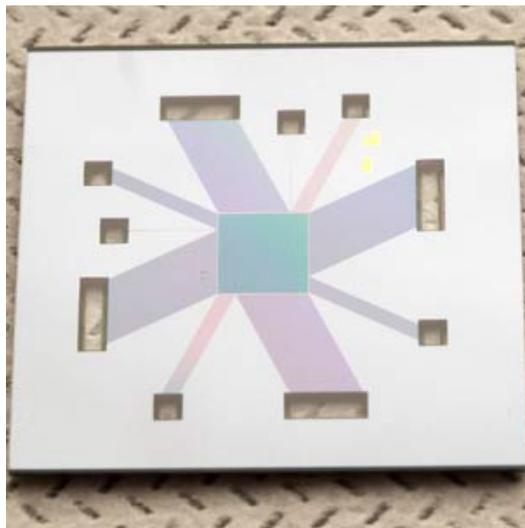
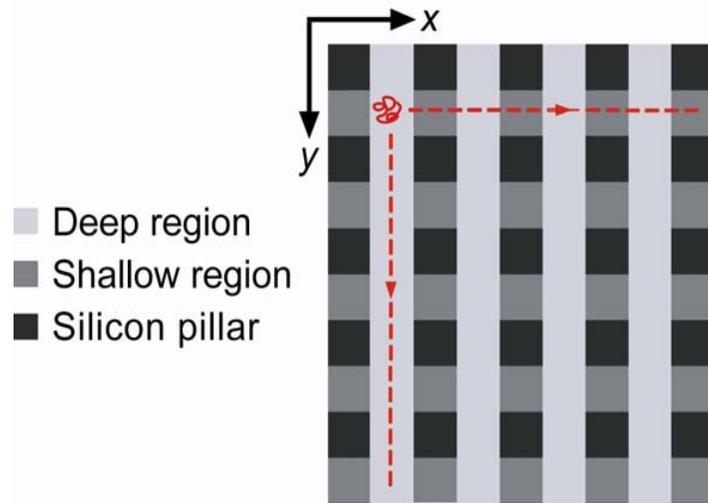
# Dielectrophoretic Manipulation of Cells

Cells trapped by dielectrophoresis, Gray et al.  
Biosensors and Bioelectronics 19 (2004) 1765–1774

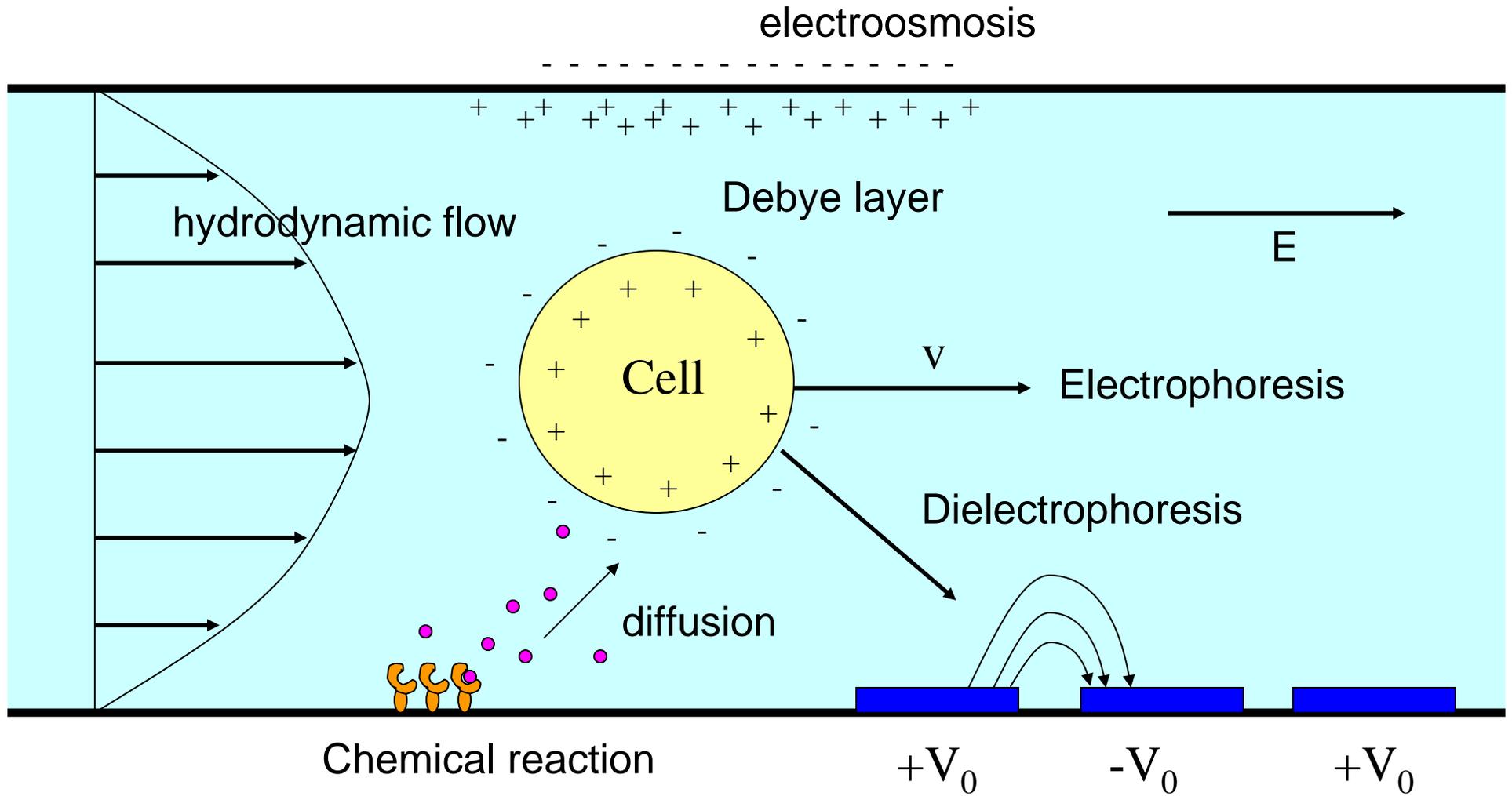
Figures removed due to copyright restrictions.

# Electrophoresis / Electrokinetics

J. Fu *et al.* *Nature Nanotechnology* (2007).  
2D anisotropic nanofilter array

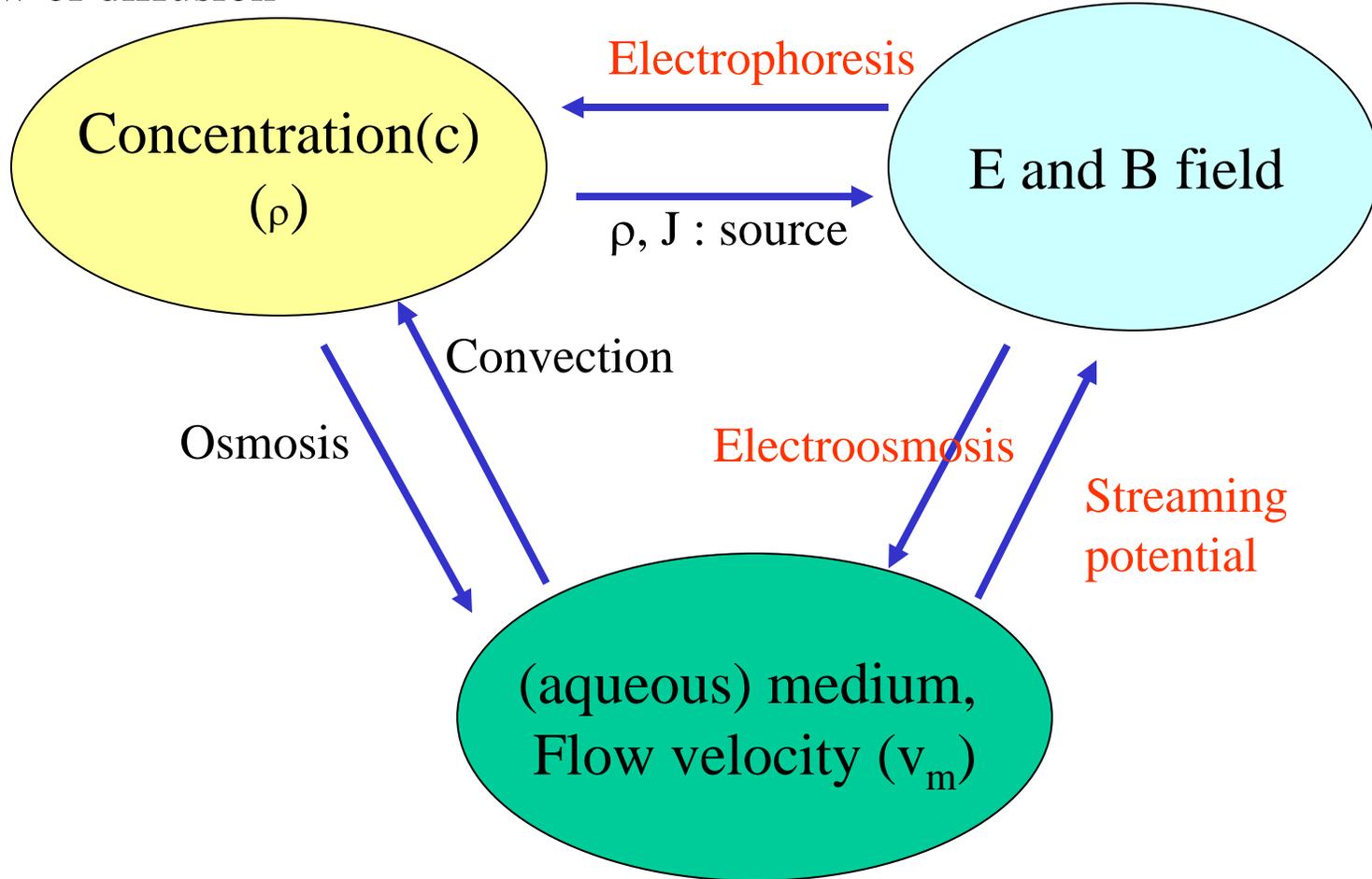


# Example : BioMEMS systems



Fick's law of diffusion

Maxwell's equation



Navier-Stokes' equation