

# Bond Prices and Yields

- Two dimensions”
  - **Default Risk** (not all issuers are alike! e.g. Argentina vs Switzerland)... poor Italian grandmothers...
  - (\*) **Maturity** (length of time over which the bond promises to make payments)
    - The Yield Curve (term structure of interest rates)
  - Figure 15-1

# Bond Prices

- A bond that promises one payment of a \$100 in n year is worth  $P_n(t)$  at time t:

$$P_n(t) = \$100 / ((1+i(t)) \cdot (1+i^e(t+n-1)))$$

If  $i$  is constant,

$$P_n(t) = \$100 / (1+i)^n$$

# The Yield Curve

- The **yield to maturity** on an n-year bond is the **constant** interest rate that makes the bond price today equal to the present value payments of the bond (sort of an “average”):

$$\$100/(1+i_n(t)) = \$100/((1+i(t)) \cdot (1+i^e(t+1)) \cdot \dots \cdot (1+i^e(t+n-1)))$$

$$\text{Approx: } i_n(t) \approx (i(t) + i^e(t+1) + \dots)/n$$

Easy example: If  $i^e(t+s) = i \Rightarrow i_n(t) = i$

Back to Figure 15-1 / Figures 15-3, 15-4, 15-5

# Stocks

- Figure 15-6
- Equity finance: dividends  $\rightarrow$  EPDV
- **$P(t) = d^e(t+1)/(1+i(t)) + d^e(t+2)/((1+i(t))(1+i^e(t+1)))+\dots$**   
**[n - > infty]**

# The Stock Market and Economic Activity

- A monetary expansion: Figure 15-7
- An increase in consumer spending: Figure 15-8
- Summary: The role of **expectations** is key.

# Bubbles

- Fundamental vs Bubbles

$$P(t) = (d^e(t+1) + P(t+1)) / (1 + i(t))$$

- Tulipmania: 1,500 guineas in 1664... to 7,500 by 1667 (the price of a house)... a few years later, 10% of the the 1667 price.
- MMM Pyramid in Russia: Sold shares promising a rate of return of 3,000% per year! In six months, P went from 1,600 rubles to 105,000 rubles... .. the company didn't produce anything! It crashed... and Mavrody became a politician...