

Department of Electrical Engineering and Computer Science  
Massachusetts Institute of Technology

6.763 Applied Superconductivity

Problem Set 7

**Problem 1:** Problem 9.1.

**Problem 2:** Problem 9.5.

**Problem 3:**

Download the files `jj.m`, `jjivh.m`, and `jjplot.m` for use with this problem set.

(a) Use `jjivh.m` to plot the IV's for a number of different Stewart-McCumber Parameters, say ( $\beta_c = 0.1, 0.5, 1, 5, 10, 15$ ). Use these to graph (1) The current where the junctions switches from the zero-voltage state to the finite voltage state as the current is increased from zero current and (2) the current where the junctions switches from the finite-voltage state to the zero-voltage state when the current is decreased from a high value. (You may note some numerical errors if you make  $\beta_c \gg 10$ , which can be resolved by increasing the integration time, but don't worry about doing this.)

(b) Use `jjplot.m` to plot the time dependence and voltage dependence for a few selected points for  $\beta_c = 0.1$  and  $\beta_c = 10$ . The program asks for an initial point  $[\phi, \dot{\phi}]$ .

(c) An often used approximation is that  $\phi(t) = \omega_0 t + A \sin(\omega_1 t + \delta)$ , where  $\omega_0$ ,  $\omega_1$ , and  $\delta$  depend on the average dc voltage. Use your results from part (b) to estimate what  $\omega_0$  and  $\omega_1$  are in terms of the average dc voltage. Note that time is in units of  $\sqrt{\tau_J \tau_{RC}}$  and the voltage is in units of  $I_C R$ .