

Subject 24.241. Logic I. Homework due Thursday, September 29.

1. For this problem, let  $N$  be the set of natural numbers (nonnegative integers), let  $E$  be the set of even natural numbers, let  $P$  be the set of primes (integers  $> 1$  that aren't divisible by any numbers other than themselves and one), and let  $S$  be the set of integers greater than 1 and less than 10.
  - a) List the members of  $S \sim P$ .
  - b) List the members of  $S \sim (P \cup E)$ .
  - c) List the members of  $P \cap E$ .
  - d) List the members of  $(S \sim P) \sim E$ .
  - e) List the members of  $S \sim (P \sim E)$ .
  
2. For this problem, let  $I$  be {Mercury, Venus, Earth, Mars}, and let  $C = \{\text{Spock, McCoy}\}$ .
  - a) List the functions from  $I$  to  $C$ , indicating which are one-one and which are onto.
  - b) How many functions are there from  $I$  to  $I$ . of these how many are one-one? Onto? Both?
  
3. Use the method of truth table to identify each of the following sentences as valid, inconsistent, or neither.
  - a)  $((P \leftrightarrow (Q \leftrightarrow R)) \leftrightarrow ((P \leftrightarrow Q) \leftrightarrow \neg R))$ .
  - b)  $((P \rightarrow Q) \rightarrow R) \rightarrow ((P \rightarrow R) \rightarrow R)$
  - c)  $((P \rightarrow (Q \vee R)) \vee ((P \rightarrow Q) \vee R))$
  
4. For each of the following categories, either give an example or explain why there can't be any example:
  - a) A tautological conditional whose antecedent is tautological.
  - b) An inconsistent conditional whose antecedent is inconsistent.
  - c) A tautological disjunction neither of whose disjuncts are tautological.
  - d) A tautological conjunction neither of whose conjuncts are tautological.
  - e) An inconsistent sentence with no negation signs.