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18.102 Introduction to Functional Analysis  
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## Lecture 2. THURSDAY, 5 FEB.

Plan:- Linear maps between normed spaces are continuous iff they are bounded. The best bound gives a norm. If the second space is Banach the space of linear operators is Banach. Corollary – the dual space of a normed space is a Banach space. Examples: Integral operators on  $\mathcal{C}^0([0, 1])$  with respect to supremum or  $L^1$  norms. Differentiation as an operator from  $\mathcal{C}^1([0, 1])$  to  $\mathcal{C}^0([0, 1])$

In practice:- I did not get to the part about differentiation.

Reading:

- (1) Wilde:- Chapter 2 to 2.7
- (2) Chen:- First part of Chapter 6 and of Chapter 7.
- (3) Ward:- Chapter 3, first 2 sections.