

2.016 HW #6  
Out: November 1, 2005  
Due: November 8, 2005

- 1) Concept questions:
- a. The majority of ocean waves are caused by what force? Discuss.
  - b. On the “Motion of a Fluid Particle” slide in the Free-Surface Waves handout, two equations are given for the velocities of a fluid particle (call him Bob):  
$$u = \frac{d\xi_p}{dt}, w = \frac{d\eta_p}{dt}$$
. What do they mean? Why are these equations valid?  
(Hint: your answer should use the words: “Eulerian” and “Lagrangian”...)
  - c. For linear deep water waves, sketch the particle orbits. How deep must a scuba diver go before he or she doesn't notice any motion due to the waves?
  - d. For linear shallow water waves, describe what a scuba diver on the bottom experiences.
- 2) For each of the following scenarios, determine whether the waves are linear or not. If so, determine the wavelength,  $\lambda$ .
- a.  $\omega = 10$  rad/s,  $H = 1$  m,  $a = 0.02$  m
  - b.  $\omega = 10$  rad/s,  $H = 0.1$  m,  $a = 0.06$  m
  - c.  $\omega = 2$  rad/s,  $H = 100$  m,  $a = 5$  m
  - d.  $\omega = 1$  rad/s,  $H = 100$  m,  $a = 2$  m
  - e.  $\omega = 5$  rad/s,  $H = 0.5$  m,  $a = 0.1$  m
  - f.  $\omega = 4$  rad/s,  $H = 0.5$  m,  $a = 0.05$  m
- 3) Consider a cylinder of radius,  $R$ , and length,  $L$ , held in place a distance,  $d$ , under the surface of the water by a slender post. The axis of the cylinder is parallel to the sea floor and perpendicular to incoming linear free-surface waves. Given  $\omega, \lambda, a$ , and  $H$ , calculate the added mass forces on the cylinder,  $F_1$  and  $F_3$ , as a function of time. (Hint: the cylinder is not moving, so the simple added mass equation applies.)
- 4) A packet of waves  $(\omega_1, k_1, a_1)$  are sent down a wavetank of height,  $H \ll \lambda_1, \lambda_2$ . A second packet  $\left(\omega_2, k_2 < k_1 \frac{\omega_2}{\omega_1}, a_2\right)$  is generated  $\tau$  seconds later. At what time will the second packet overtake the first?
- 5) Compare and contrast the vertical Foude-Krylov force to the restoring force due to buoyancy. What causes each force, and why are they different?