

by symmetry

$$q_1 = q_3 = q_7 = q_9$$

ORIGIN := 1

$$q_2 = q_4 = q_6 = q_8$$

$$\eta_{ij} = \sum_{j=1}^4 \frac{s_{ij}}{t_{ij}} \quad \eta_{ik} = \frac{s_{ik}}{t_{ik}}$$

$$\eta_{1,1} := 4 \cdot \frac{a}{t} \quad \eta_{1,2} := 2 \cdot \frac{a}{t} \quad \text{by symmetry } q_4=q_2 \text{ so } q_1 \text{ has } 2 \cdot a \text{ length in common with } q_2$$

$$\eta_{2,1} := 2 \cdot \frac{a}{t} \quad \eta_{2,2} := 4 \cdot \frac{a}{t} \quad \eta_{2,5} := \frac{a}{t} \quad \text{by symmetry } q_3=q_1 \text{ so } q_2 \text{ has } 2 \cdot a \text{ length in common with } q_1 \text{ 1nd } 1 \cdot a \text{ in common with } q_5$$

$$\eta_{5,2} := 4 \cdot \frac{a}{t} \quad \eta_{5,5} := 4 \cdot \frac{a}{t} \quad \text{by symmetry } q_4=q_6=q_8=q_2 \text{ so } q_5 \text{ has } 4 \cdot a \text{ length in common with } q_2$$

$$\begin{pmatrix} \eta_{1,1} & -\eta_{1,2} & 0 \\ -\eta_{2,1} & \eta_{2,2} & -\eta_{2,5} \\ 0 & -\eta_{5,2} & \eta_{5,5} \end{pmatrix} \cdot \begin{pmatrix} q_{\text{bar}_1} \\ q_{\text{bar}_2} \\ q_{\text{bar}_5} \end{pmatrix} = \begin{pmatrix} a^2 \\ a^2 \\ a^2 \end{pmatrix}$$

$$\begin{pmatrix} q_{\text{bar}_1} \\ q_{\text{bar}_2} \\ q_{\text{bar}_5} \end{pmatrix} := \begin{pmatrix} \eta_{1,1} & -\eta_{1,2} & 0 \\ -\eta_{2,1} & \eta_{2,2} & -\eta_{2,5} \\ 0 & -\eta_{5,2} & \eta_{5,5} \end{pmatrix}^{-1} \cdot \begin{pmatrix} a^2 \\ a^2 \\ a^2 \end{pmatrix}$$

$$q_{\text{bar}} \rightarrow \begin{pmatrix} \frac{11}{16} \cdot a \cdot t \\ \frac{7}{8} \cdot a \cdot t \\ 0 \\ 0 \\ \frac{9}{8} \cdot a \cdot t \end{pmatrix}$$

we need to account for all the cells in calculating J or q from the known q_bar

$$i := 1..9$$

A · q_bar does the sum in mathcad

$$q_{\text{bar}} := \begin{pmatrix} q_{\text{bar}_1} \\ q_{\text{bar}_2} \\ q_{\text{bar}_1} \\ q_{\text{bar}_2} \\ q_{\text{bar}_5} \\ q_{\text{bar}_2} \\ q_{\text{bar}_1} \\ q_{\text{bar}_2} \\ q_{\text{bar}_1} \end{pmatrix}$$

$$A_i := a^2$$

aside ...

$$J := 4 \cdot A \cdot q_{\text{bar}}$$

$$J \rightarrow \frac{59}{2} \cdot a^3 \cdot t$$

$$q_i := T \cdot \frac{q_{\text{bar}_i}}{2 \cdot A \cdot q_{\text{bar}}}$$

$$\begin{pmatrix} q_1 \\ q_2 \\ q_5 \end{pmatrix} \rightarrow \begin{pmatrix} \frac{11}{236} \cdot \frac{T}{a^2} \\ \frac{7}{118} \cdot \frac{T}{a^2} \\ \frac{9}{118} \cdot \frac{T}{a^2} \end{pmatrix}$$

and ...

$$q_{12} := q_1 - q_2$$

$$q_{12} \rightarrow \frac{-3}{236} \cdot \frac{T}{a^2}$$

negative means it is down (- as seen from cell 1)

$$q_{25} := q_2 - q_5$$

$$q_{25} \rightarrow \frac{-1}{59} \cdot \frac{T}{a^2}$$

negative means it is to the left (- as seen from cell 2)