

# Assembly System Design Techniques

- Goals of this class
  - Introduce system design methods
  - Understand the things that must be considered
  - Look at two ways to approach it
  - Learn about SelectEquip

# Assembly System Design Techniques

- Assembly system design algorithms exist
- They solve the “Equipment Selection and Task Assignment” problem
- Methods include dynamic programming, travelling salesman, mixed integer-linear programming, and a heuristic called ASDP
- These algorithms will design an assembly or other process line to meet average production requirements, adjusted for a fixed % uptime
- Detailed simulation is needed to verify production rate and study queues and other issues

# What to Model

- The tasks that need to be done
- The number of units needed per year
- What resources are available or applicable to a given task
  - What each resource costs to buy
  - What tool it needs for each task
  - How long it will take to do the task, change tools, etc
  - What is its uptime and other operating characteristics
- Time for transport from station to station
- Reuse of a resource for several tasks
- Reuse of tools at one station

# History

- Heuristics by R E Gustavson at Draper and N H Cook at MIT in 1970s
- Solutions based on OR techniques by Prof Graves and OR Center students
  - Terry Huttner, 1977 - mixed linear-integer programming
  - Bruce Lamar, 1979 - bus routing algorithm
  - Carol Holmes, 1987 - multiple products, dynamic programming
  - Curt Coopriider, 1989 - uncertain demand, dynamic programming
- Holmes-Coopriider method reprogrammed by Mike Hoag, 2001.

# System Selection Criteria

- Minimize annualized cost
  - = unit labor cost + annualized cost of capital
- Systems can be forced to be all manual, all robot, or all fixed automation just by removing unwanted resource classes
- A wide variety of preferences can be accommodated this way

# Summary of Required Input

- Info about assembly resources with cost, operation time, and “rho” or installed cost factor
  - rho relates total cost to equipment cost
- Info about assembly tasks with operation time and tool number for each resource
- Annual production volume, labor cost, min acceptable rate of return, number of shifts available
  - Rate of return expressed in annualized cost factor

# Data Input (Applicable Technology Chart)

Title			Date
Working days/year		Annualized cost factor	
Shifts available		Avg loaded labor rate (\$/hr)	
	Station-station move time (s)		
Resource data set name:		Task data set name:	
	For each resource:	When a resource can be used:	
C	hardware Cost (\$)		
rho	installed cost/hardware cost	Operation	Tool
e	% uptime expected	time (s)	number
v	operating/maintenance rate (\$/hr)		
Tc	Tool change time (s)	Hardware cost	
Ms	Max # stations/worker		
NOTE: SEE FIG 14.8 OF CONCURRENT DESIGN AND PP 434-435			
Resource:			
.....	C _____	C _____	C _____
.....	rho _____	rho _____	rho _____
.....	e _____	e _____	e _____
.....	v _____	v _____	v _____
.....	Tc _____	Tc _____	Tc _____
Task:	Ms _____	Ms _____	Ms _____
1			
2			
3			
4			
5			
6			
7			
8			
9			
10			



TITLE MECHANISM SUB-ASSEMBLY DATE 10 FEB. 1984

228 WORKING DAYS PER YEAR      .3682 ANNUALIZED COST FACTOR  
1 or 3 SHIFTS AVAILABLE      13 AVERAGE LOADED LABOR RATE (\$/h)  
2 s STATION-TO-STATION MOVE TIME

RESOURCE DATA SET NAME: RES14      TASK DATA SET NAME: RECBI

FOR EACH RESOURCE:

- C: HARDWARE COST (\$)
- p: INSTALLED COST/HARDWARE COST
- e: UP-TIME EXPECTED (%)
- v: OPERATING/MAINTENANCE RATE (\$/h)
- t<sub>c</sub>: SECONDS TOOL CHANGE TIME
- m<sub>s</sub>: MAXIMUM STATIONS PER WORKER

WHEN A RESOURCE CAN BE USED ON A TASK:

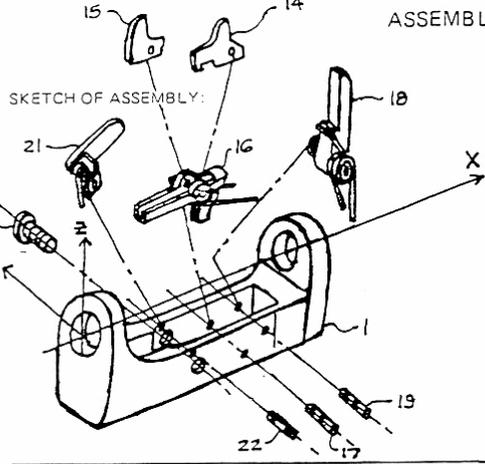
OPERATION TIME (s) | TOOL NUMBER  
 -----  
 HARDWARE COST (\$)

TASK NUMBER	M13		P29		F30		F60	
	C:	m <sub>s</sub> :	C:	m <sub>s</sub> :	C:	m <sub>s</sub> :	C:	m <sub>s</sub> :
1. Part 14	200	833	25000	6	0	6	0	4
2. Part 15	1.5		3.5		1.5		1.5	
3. Part 16	80		80		80		80	
4. Part 17	.88		.75		.60		.50	
5. Part 18	2		3		0		0	
6. Part 19	2000		7000		15000		60000	
7. Part 20	5	111	4	211	3	311	2	411
8. Part 21	30	112	20	212	15	312	10	411
9. Part 22	10	113	6	213	4	312	2	411
	4000		10000		40000		60000	
	60	114	<del>X</del>		<del>X</del>		20	412
	1500		5000		40000		60000	
	10	113	6	213	4	313	2	412
	1500		5000		15000		60000	
	10	111	6	211	4	314	2	413
	2000		7000		15000		60000	
	25	112	15	212	12	315	10	413
	4000		10000		30000		60000	
	10	113	6	213	4	315	2	413
	1500		5000		30000		60000	

	UNITS	DAYS
PRODUCTION	<u>60000</u>	<u>228</u>
BATCH	<u>180000</u>	<u>228</u>
DATA	<u>600000</u>	<u>228</u>
	y	11/16/2004

Applicable Technology Chart

# Assembly Planning Chart



NAME: MECHANISM SUB-ASSEMBLY

DATE: 10 FEB. 1984

PREPARED BY: REG

SHEET 1 OF 1

TASK	SEQUENCE	TYPE OF TASK	BASIC ORIENTATION	MOTION(S) REQUIRED	JIGGING/TOOLING REQUIRED	DEGREE OF DIFFICULTY OF TASK	INSPECTION REQUIRED	CYCLE TIME (s)	COMMENTS
Pickup Part 14.	1		X-Z	X, Z		1			
Pickup Part 15.	2		X-Z	X, Z		1			
Assemble both into Part 16.		P	X-Z	-Z		2			
Install into Part 1.	3	A	X-Z	-Z	Y	3	C		Must be aligned
Push in Part 17.	4	I	Y-Z	Y		2	C		Check motion
Get Part 18.			X-Z			1			
Position inside part 1.	5	A	X-Z	X, Z	Y	4	C		Must be aligned
Push in Part 19.	6	I	Y-Z	Y		2	C		Check motion
Get Part 20.			Y-Z			1			
Install in part 1.	7	I	Y-Z	-Y		1			
Get Part 21			X-Z			1			
Position inside part 1.	8	A	X-Z	-Z	Y	3	C		Must be aligned
Push in Part 22	9	I	Y-Z	Y		2	C		Check motion

ABBREVIATIONS USED:

P - PLACE, ORIENT	B - BOLT TORQUE
T - TIGHTEN BOLTS, NUT, etc.	G - GAUGE DIMENSION
I - INSERT PARTS	C - COMPARISON
M - MEASURE	
S - SHAPE MODIFY	
A - ALIGN	

# Basic Nominal Capacity Equations

# operations/unit \* # units/year = # ops/yr

# ops/sec = # ops/yr \* (1 shift/28800 sec)\*(1 day/n shifts)\*(1 yr/280 days)

cycle time = 1/(ops/sec) = required sec/op

equipment capability = actual sec/op

actual sec/op < required sec/op -> happiness

required sec/op < actual sec/op -> misery (or multiple resources)

Typical cycle times: 3-5 sec manual small parts

5-10 sec small robot

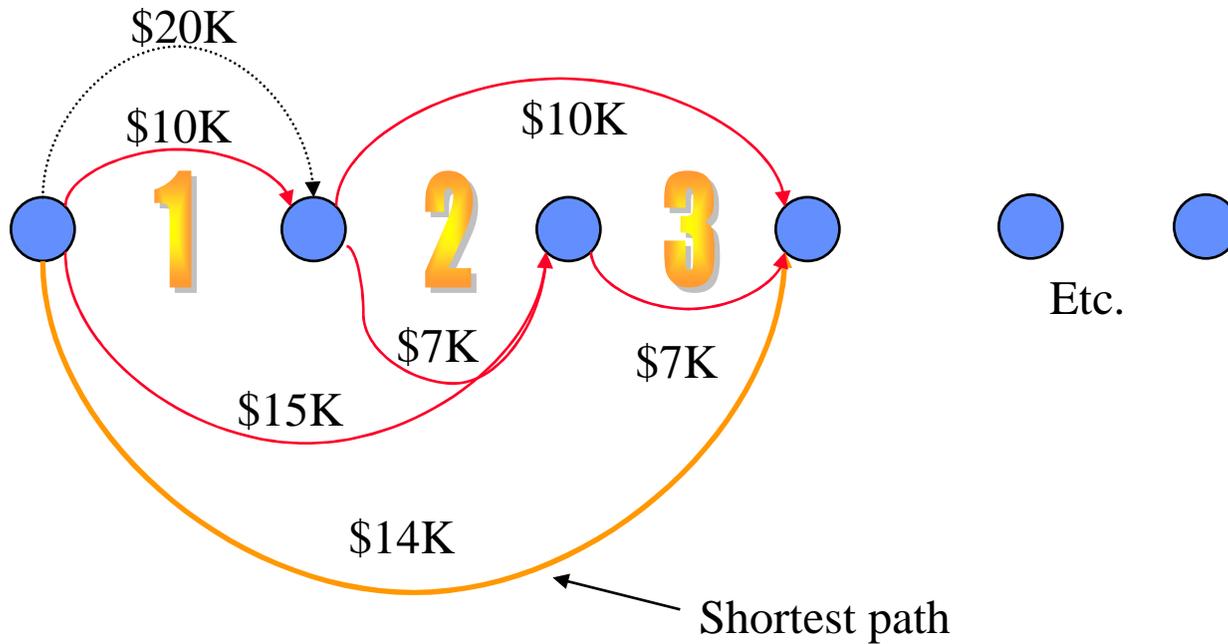
1-4 sec small fixed automation

10-60 sec large robot or manual large parts

# How the Holmes-Coopriider Method Works

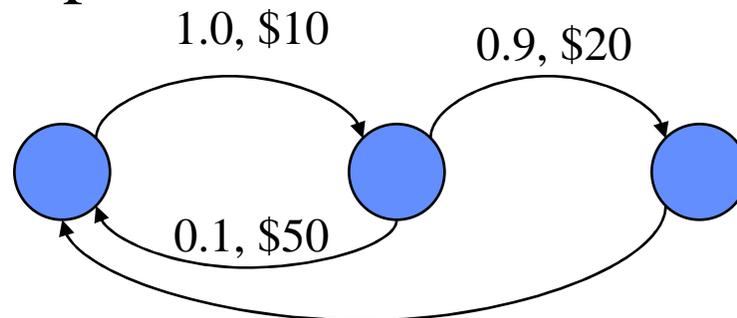
- The maximum takt or cycle time is calculated based on annual volume requirement and # shifts
- Each resource is tested to see if it can do one task without running out of time, two tasks, three tasks, etc.
- A network is built where pairs of nodes are tasks, and arcs are resources
- Each arc has a cost based on investment, tools, and labor (labor cost based on time used)
- The shortest path through the network is the string of selected resources and the tasks they will do

# Network



# Network Models of Assembly Systems

- Model of system as flows in a network
- Represents equilibrium state
- Based on probabilities and costs



- Outbound probabilities add to 1.0
- Equilibrium solution gives average cost to go through and average flow on each branch

# Equations

$p_{ij}$  = pr of going from node i to node j

$c_{ij}$  = cost of going from node i to node j

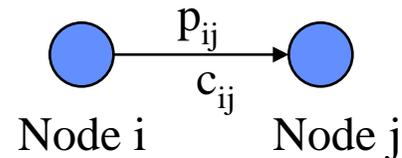
$f_{ij}$  = flow from node i to node j

$y_i$  = total flow out of node i

$$f_{ij} = y_i p_{ij}$$

where we must have

$$\sum_j p_{ij} = 1 \text{ for each } i$$



Conservation of flow at node j:

$$y_j = y_j p_{jj} + \sum_{k \neq j} y_k p_{kj} + x_j \longrightarrow$$

$x_j$  = flow into node j from outside

$$p_{jj} = 0$$

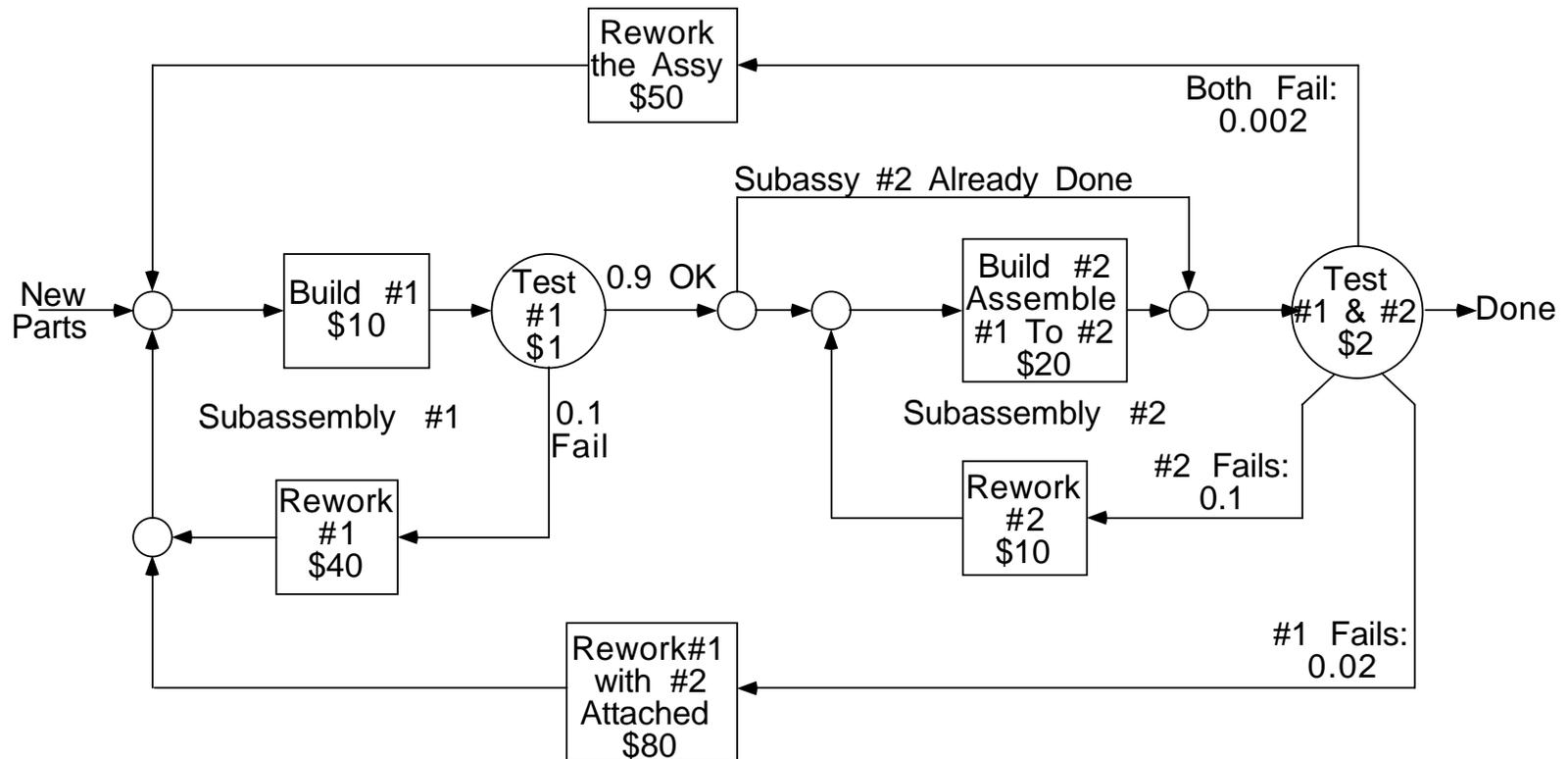
Solution:

$$Y = P^T Y + X$$

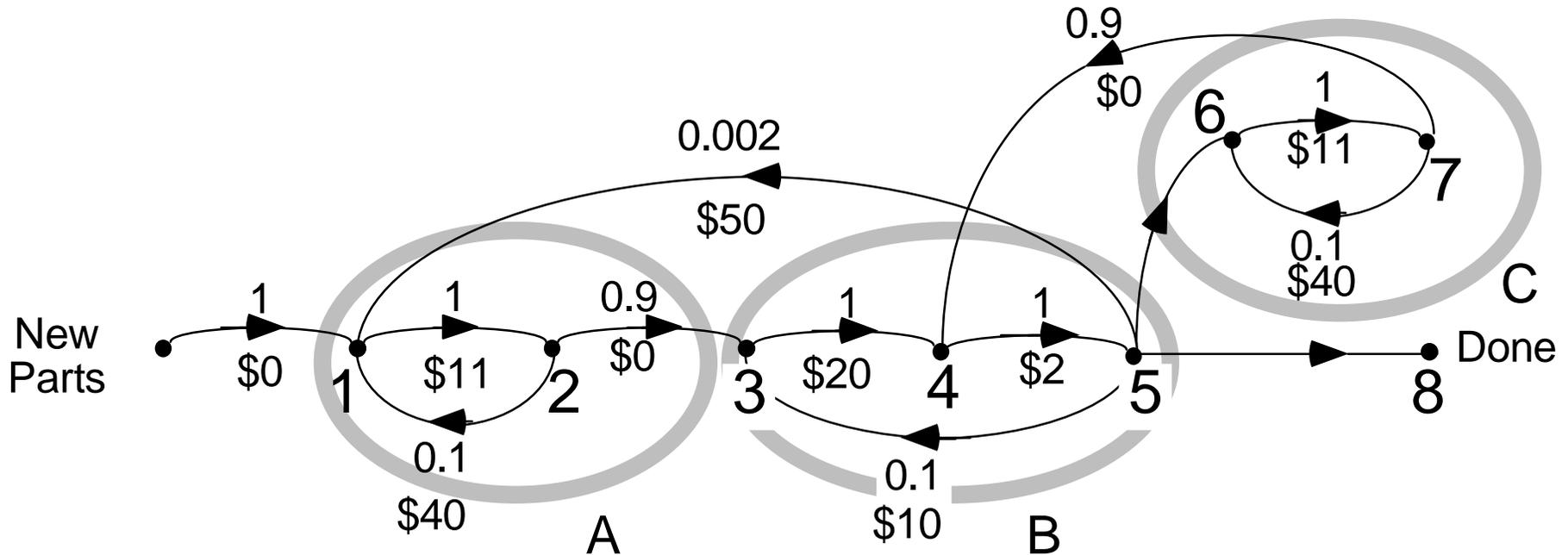
$$Y = [I - P^T]^{-1} X$$

$$cost = \sum_i \sum_j f_{ij} c_{ij}$$

# Example System: an assembly with two subassemblies and several test and rework stations



# Network Equivalent of Example



- A Build/repair Subassembly #1 and Test it
- B Build/repair Subassembly #2 and Test Both
- C Repair/rebuild #1 While Attached to #2

# Matlab Solution

```
»P=zeros(8)
»C=zeros(8)
%Arc probabilities:
»P(1,2)=1;
»P(2,1)=.1;
»p(2,3)=.9;
»P(2,3)=.9;
»P(3,4)=1;
»P(4,5)=1;
»P(5,3)=.1;
»P(5,1)=.002;
»P(5,6)=.02;
»P(5,8)=1-P(5,6)-P(5,3)-P(5,1);
»P(6,7)=1;
»P(7,4)=.9;
»P(7,6)=.1;
»X=[1 0 0 0 0 0 0 0];
»X=X'
»Y=inv(eye(8)-P')*X
Y =
1.1136
1.1136
1.1162
1.1390
1.1390
0.0253
0.0253
1.0000
»YY=[Y Y Y Y Y Y Y Y]
»F=box(YY,P)
```

# Equilibrium Flows

F =

0.0000	1.1136	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
0.1114	0.0000	1.0023	0.0000	0.0000	0.0000	0.0000	0.0000
0.0000	0.0000	0.0000	1.1162	0.0000	0.0000	0.0000	0.0000
0.0000	0.0000	0.0000	0.0000	1.1390	0.0000	0.0000	0.0000
0.0023	0.0000	0.1139	0.0000	0.0000	0.0228	0.0000	1.0000
0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0253	0.0000
0.0000	0.0000	0.0000	0.0228	0.0000	0.0025	0.0000	0.0000
0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000

# Cost Solution

% Arc costs:

$$\gg C(1,2)=11;$$

$$\gg C(2,1)=40;$$

$$\gg C(3,4)=20;$$

$$\gg C(4,5)=2;$$

$$\gg C(5,1)=50;$$

$$\gg C(5,3)=10;$$

$$\gg C(5,3)=10;$$

$$\gg C(5,6)=80;$$

$$\gg C(6,7)=11;$$

$$\gg C(7,6)=40;$$

$$\gg \text{cost}=\text{sum}(\text{sum}(\text{box}(C,F)))$$

cost =

\$44.7608

Cost without rework = \$33

%FF = total flow in system

$$\gg \text{FF}=\text{sum}(\text{sum}(F))$$

$$\gg \text{FF}=5.6720$$

%EX=excess flow

$$\gg \text{EX}=\text{FF}/5$$

EX =

1.1344

Total flow without rework = 5

Capacity devoted to rework = 13.44%