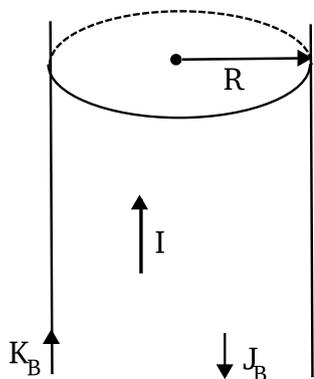


8.022 Lecture Notes Class 26 - 10/31/2006



Long copper wire of radius  $R$ ,  
uniform current  $I$

Find:

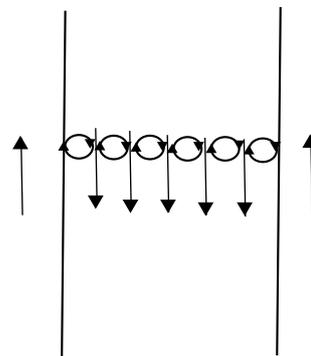
1. Direction of bound currents  
 $\frac{\vec{J}_B}{|\vec{J}_B|}$ ,  $\frac{\vec{k}_B}{|k_B|}$
2.  $\vec{H}$  inside
3.  $\vec{H}$  outside

What's a bound current? One way: electrons in materials moving  
Current that cannot escape; property of material.

$$\oint \vec{H} \cdot d\vec{l} = I_{\text{free enclosed}}$$

$$\begin{aligned} \vec{H} &= \frac{I}{2\pi r} \\ \vec{J}_B &= \vec{\nabla} \times \vec{M} \\ &= \vec{\nabla} \times \left(\frac{\vec{m}}{V}\right) \dots? \end{aligned}$$

$\hat{J}_B$  is down because little circles of  
current cancel out inside to go  
down, on surface  $\vec{k}_B$  goes up



1.

2. Well,  $H$  depends only on free current

Inside:

$$\oint \vec{H} \cdot d\vec{l} = I_{\text{freeenclosed}} \qquad \vec{\nabla} \times \vec{H} = \vec{J}_{\text{free}}$$

$$H = \frac{1}{2\pi r} \cdot I \cdot \frac{\pi r^2}{\pi R^2} = \frac{Ir}{2\pi R^2} \hat{\phi} \qquad \vec{H} = \frac{1}{\mu_0} \vec{B} - \vec{M}$$

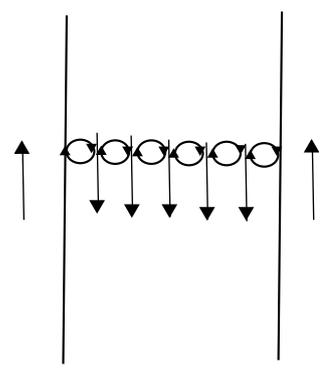
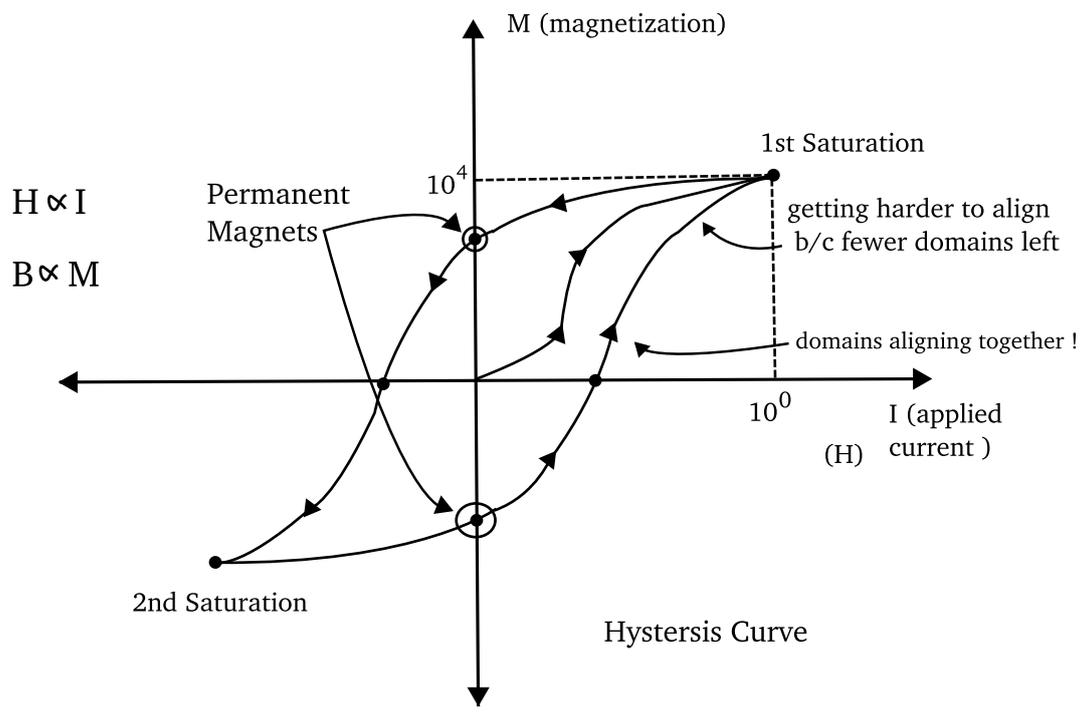
3. Outside :

$$\oint \vec{H} \cdot d\vec{l} = I_{\text{freeenclosed}}$$

$$H = \frac{I}{2\pi r} \hat{\phi}$$

### Ferromagnetism

- based on history
  - aligns with itself
  - rare - requires special electronic structure
  - nonlinear
- Ferromagnetic domains align to external fields



We know this creates an  $\vec{H}$ , which is related to  $\vec{M}$

Curie pt:  $10^3 K$  (Ferro  $\rightarrow$  para )