

# Electricity and Magnetism

- Electric field continued

# Electric Field

- New concept – Electric Field  $\vec{E}$
- Charge  $Q$  gives rise to a Vector Field

$$\vec{E}(\vec{x}) = \vec{F}(\vec{x})/q$$

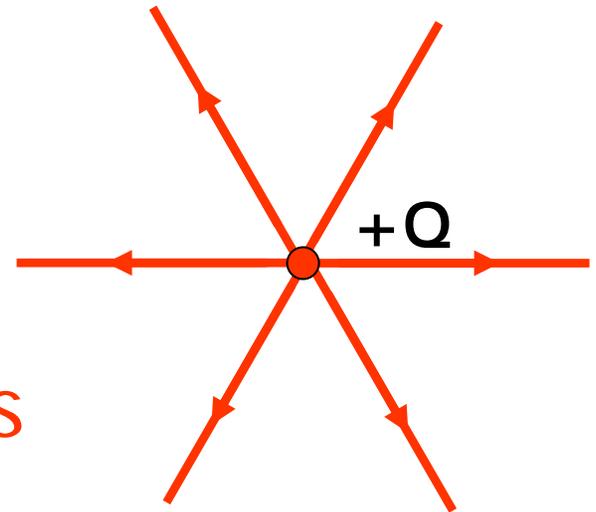
- $\vec{E}$  is defined by strength and direction of force on small test charge  $q$

# Electric Field

- For a single charge

$$E = k \frac{Q}{r^2}$$

- Visualize using Field Lines
  - Cartoon!
  - Strength -> Density of Lines
  - Direction -> Direction of Lines
    - away from positive charges



# Electric Field

- Field can be used to accelerate charged particles

$$\mathbf{F} = \mathbf{Q E}$$

-> Particle Accelerators

# The Electric Field

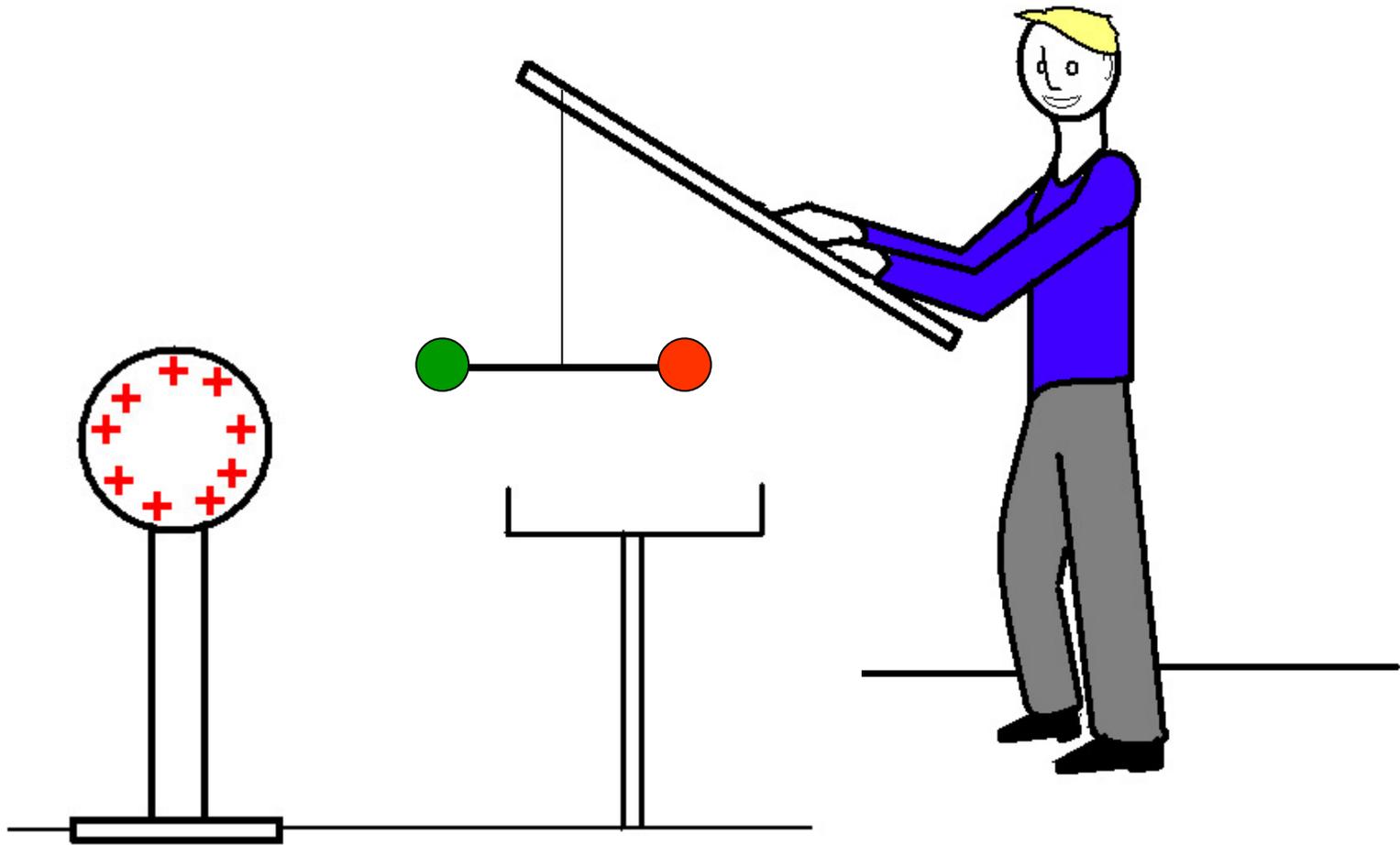
- Electric Field also exists is test charge  $q$  is not present
- We can say:

**The charge  $Q$  gives rise to a property of space itself – the Electric Field**

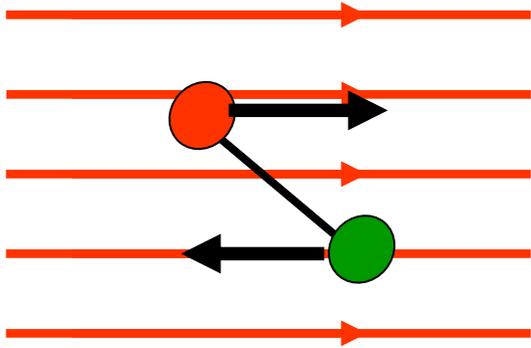
**-> In-Class Demo...**

# Electric Field Demo

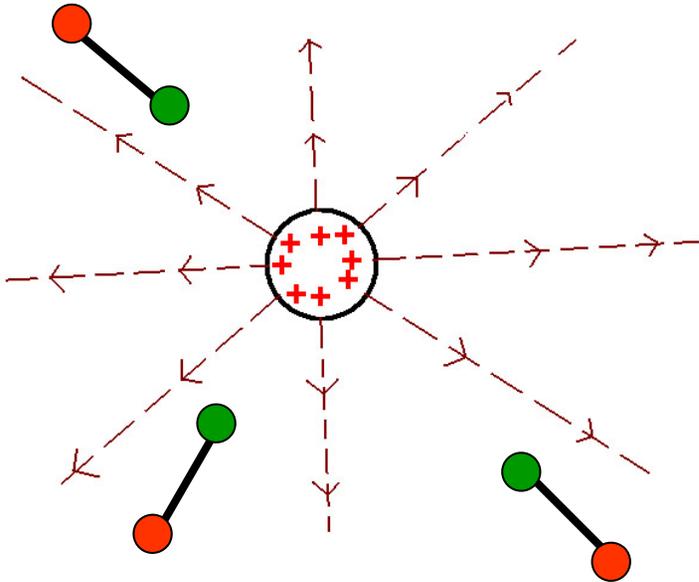
- Use a **Van-der-Graaf Generator**
- Much more powerful than rubbing glass rods
- Not really dangerous (I've been told) – but potentially painful
- Creates large electric fields
- Really big ones were used in Particle Accelerators (still in use in some labs)



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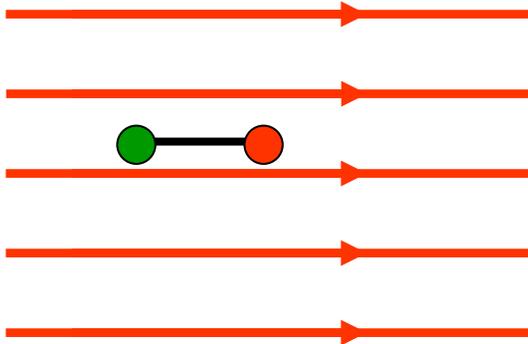


Torque  $\vec{\tau} = \vec{p} \times \vec{E}$   
 $\vec{p} = Q l$  Dipolemoment

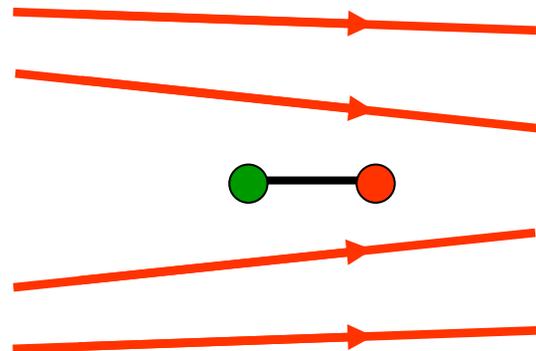


# Does Dipole feel a net Force?

No

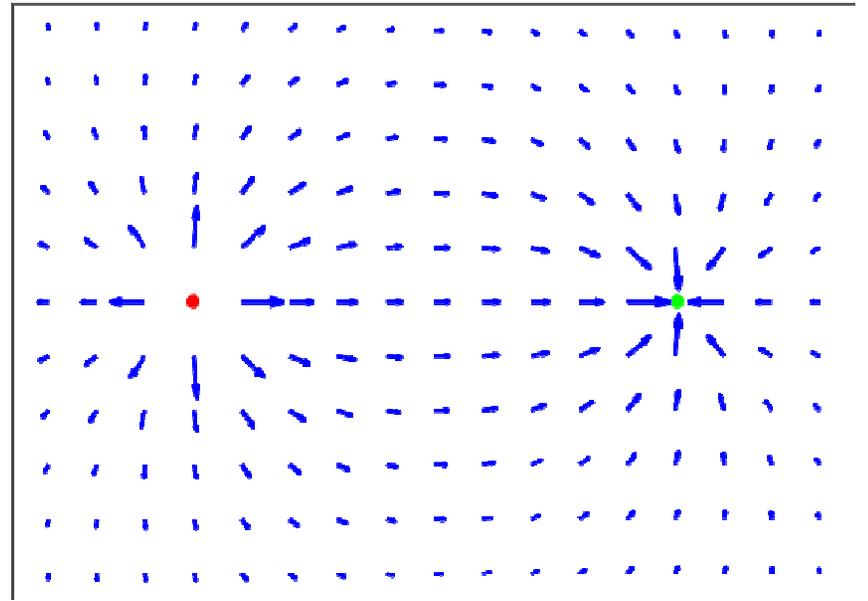
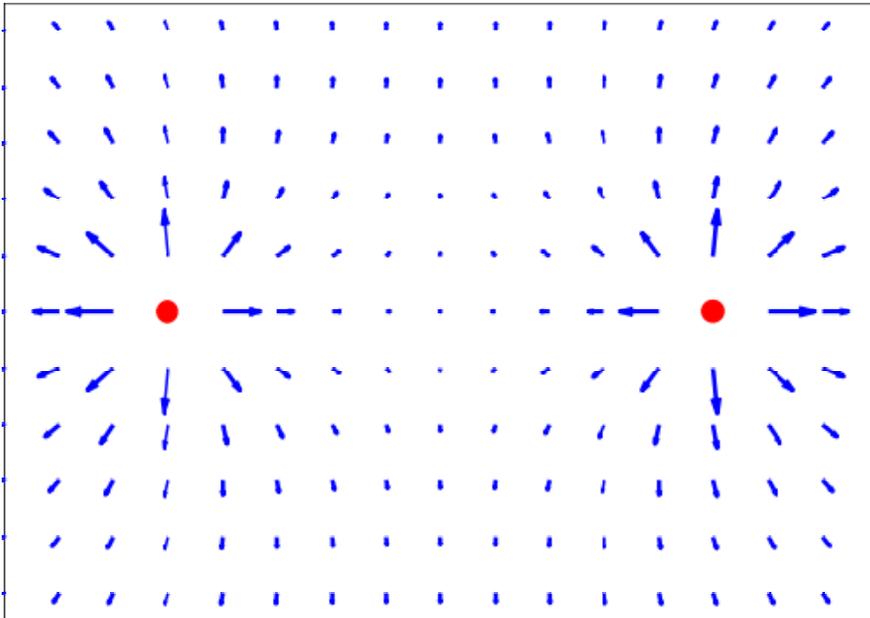


Yes

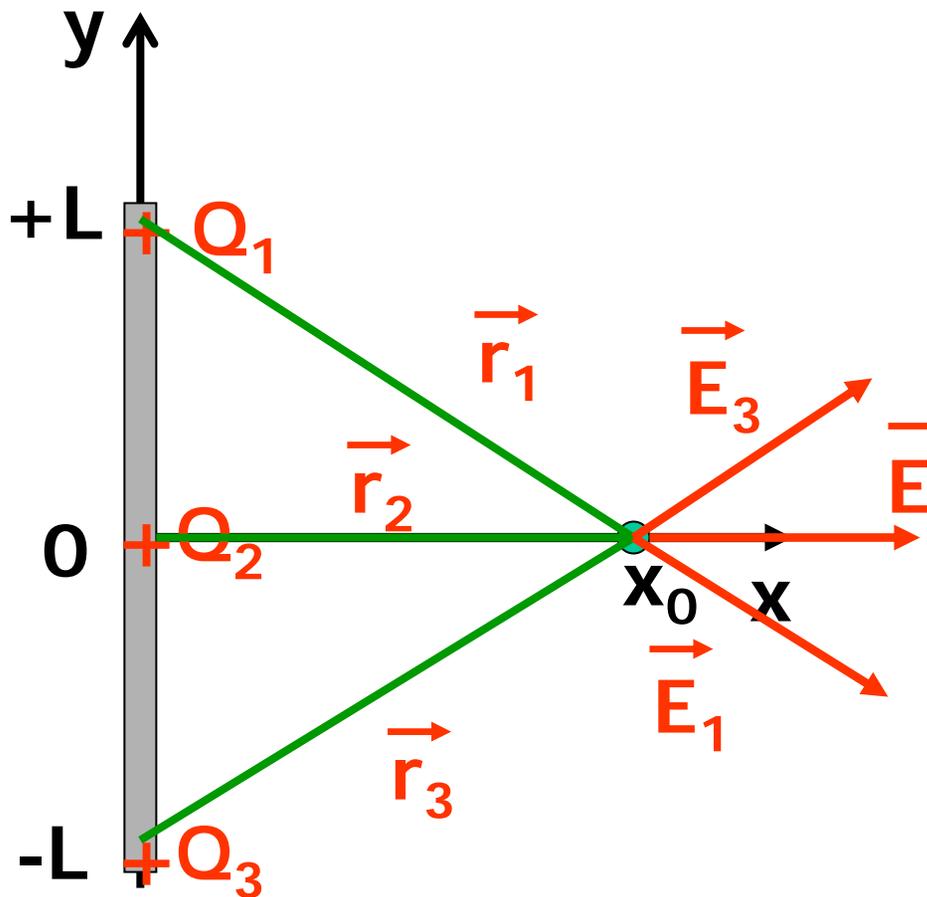


# Superposition Principle

- Field of many charges is Vector Sum of individual fields



# Example: Superposition principle for 3 charges



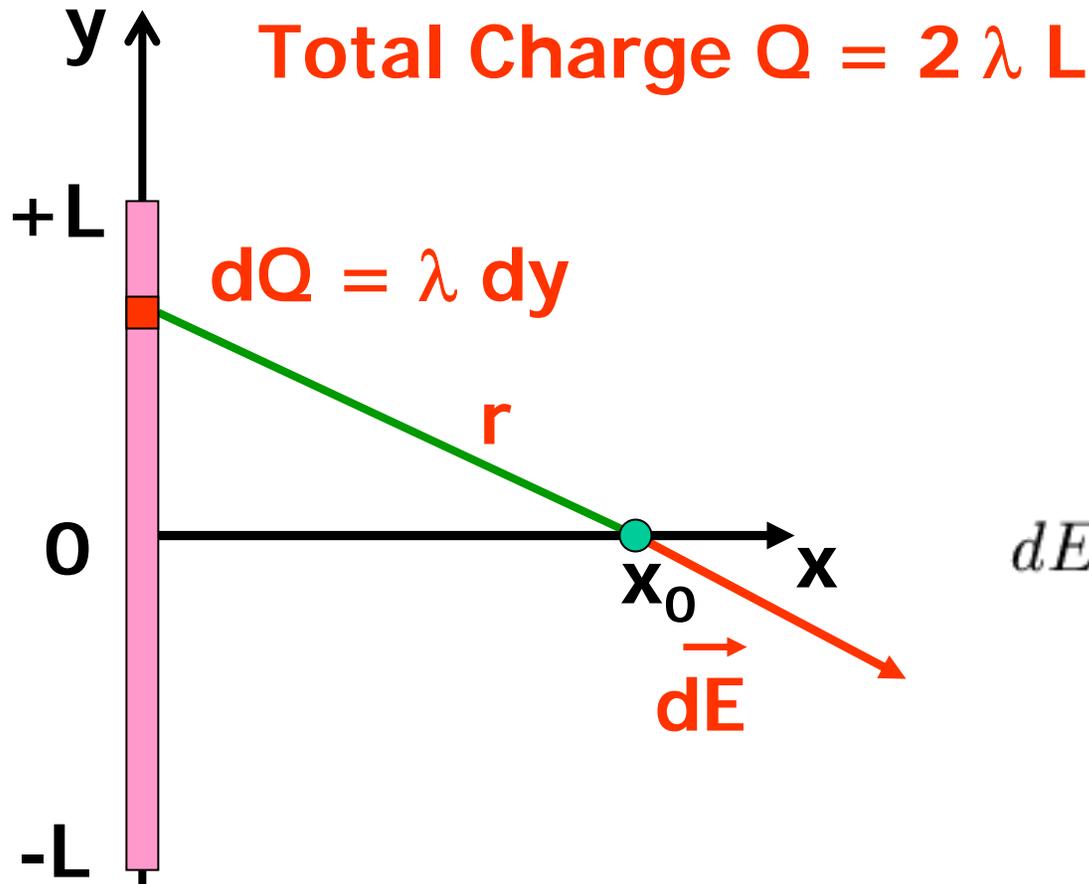
$$\vec{E}_i = k \frac{Q_i}{r_i^2} \hat{r}_i$$

$$E_{y,total} = 0$$

$$E_{i,x} = E_i \cos(\Theta) = E_i \frac{x_0}{x_0^2 + y_i^2}$$

$$\begin{aligned} E_x &= \sum E_{i,x} \\ &= kQ \cdot \left( \frac{1}{x_0^2} + \frac{2x_0}{(x_0^2 + L^2)^{3/2}} \right) \end{aligned}$$

# Example: Superposition principle for continuous charge distribution



$$d\vec{E} = k \frac{dQ}{r^2} \hat{r}$$

$$\begin{aligned} dE_x &= k \frac{dQ}{x_0^2 + y^2} \cos(\Theta) \\ &= k \frac{dQ}{x_0^2 + y^2} \frac{x_0}{\sqrt{x_0^2 + y^2}} \\ &= k \lambda dy \frac{x_0}{(x_0^2 + y^2)^{3/2}} \end{aligned}$$

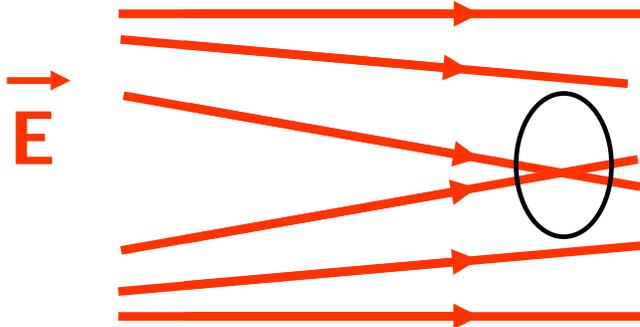
# Example: Superposition principle for continuous charge distribution

$$\begin{aligned}\vec{E} &= E_x \hat{x} \\ &= \int_{\text{all charge}} dE_x \\ &= k\lambda x_0 \int_{-L}^{+L} \frac{dy}{(x_0^2 + y^2)^{3/2}}\end{aligned}$$
$$\begin{aligned}d\vec{E} &= k \frac{dQ}{r^2} \hat{r} \\ dE_x &= k \frac{dQ}{x_0^2 + y^2} \cos(\Theta) \\ &= k \frac{dQ}{x_0^2 + y^2} \frac{x_0}{\sqrt{x_0^2 + y^2}} \\ &= k\lambda dy \frac{x_0}{(x_0^2 + y^2)^{3/2}}\end{aligned}$$

$$E_x = 2k\lambda \frac{L}{x_0 \sqrt{x_0^2 + L^2}}$$

# More on Fields and Field Lines

- What's wrong with this picture?
- Magnitude and direction of field have to be unique at each point!
- Field lines can't cross!



# More on Fields and Field Lines

- Very close to surface of charged object
- Field lines perpendicular to surface (if we go close enough)!
- Symmetry left and right (like an infinite plane)

