8.325 Homework 7

Iain Stewart, May 6, 2007 Due: Thur. May 17.

Problem 1) Some algebra used to study θ -vacua and instantons

a) Let $\tilde{G}^{\mu\nu} = \epsilon^{\mu\nu\alpha\beta} G_{\alpha\beta}$ and

$$K^{\mu} = 2\epsilon^{\mu\alpha\beta\gamma} \text{Tr} \left[G_{\alpha\beta} A_{\gamma} + \frac{2i}{3} A_{\alpha} A_{\beta} A_{\gamma} \right]$$
 (1)

and show that $\partial_{\mu}K^{\mu} = \text{Tr}[G_{\mu\nu}\tilde{G}^{\mu\nu}]$. Feel free to use the Bianchi identity, $D_{\mu}\tilde{G}^{\mu\nu} = 0$, without proof.

b) Show that the instanton

$$A_{\mu} = \frac{r^2}{r^2 + \rho^2} (-i) g^{\dagger} \partial_{\mu} g, \qquad g = \frac{x_4 + i\vec{x} \cdot \vec{\sigma}}{r}$$
 (2)

where $r^2 = x_4^2 + \vec{x}^2$ satisfies the Euclidean field equations $D_{\mu}G^{\mu\nu} = 0$.

Problem 2) Scalar production, $e^+e^- \rightarrow q\bar{q}S$

Peskin & Schroeder, page 596, Problem 17.2, part a).

Problem 3) Deep inelastic scattering from a photon.

Peskin & Schroeder, page 649, Problem 18.4 parts a), b), c).