

Angry Madness: Payoff Detail

Your overall payoff will be determined by averaging your payoff in each of the 9 cases when you and your have $M, U = 100, 200, \text{ or } 400$. Your expected payoff in each of these 9 cases is, in turn, calculated by checking every possible way that the game might end.

Bart's expected payoff when $M = \$200$ for Ann and $U = \$200$ for Bart

We add up all of the terms below, which correspond to all ways the game might end:

First round, Bart yields	$50\% * \$200$	= 100
First round, Ann yields	$0\% * \$300$	
First round, both yield	$0\% * \$200$	
Anger after First round	$50\% * 10\% * \$0$	

(Note: Chances we go on to second round = $P1 = 50\% * 90\%$.)

Second round, Bart yields	$P1 * 25\% * \$200$	= 22.5
Second round, Ann yields	$P1 * 0\% * \$300$	
Second round, both yield	$P1 * 0\% * \$200$	
Anger after Second round	$P1 * 75\% * 20\% * \$0$	

(Note: Chances we go on to third round = $P2 = 50\% * 90\% * 75\% * 80\%$.)

Third round, Bart yields	$P2 * 75\% * \$200$	= 40.5
Third round, Ann yields	$P2 * 0\% * \$300$	
Third round, both yield	$P2 * 0\% * \$200$	
Anger after Third round	$P2 * 25\% * 30\% * \$0$	

(Note: Chances we go to fourth round = $P3 = 50\% * 90\% * 75\% * 80\% * 25\% * 70\%$.)

Third round, Bart yields	$P2 * 100\% * \$200$	= 9.45
Third round, Ann yields	$P2 * 0\% * \$300$	
Third round, both yield	$P2 * 0\% * \$200$	
Anger after Third round	$P2 * 0\% * 40\% * \$0$	

Bart's Expected Payoff = 172.45

... Bart would have been better off yielding for sure in Round 1 (which gives guaranteed payoff 200)

Ann's expected payoff when $M = \$200$ for Ann and $U = \$200$ for Bart

We add up all of the terms below, which correspond to all ways the game might end:

First round, Bart yields	$50\% * \$300$	= 150
First round, Ann yields	$0\% * \$200$	
First round, both yield	$0\% * \$200$	
Anger after First round	$50\% * 10\% * \$0$	

(Note: Chances we go on to second round = $P1 = 50\% * 90\%$.)

Second round, Bart yields	$P1 * 25\% * \$300$	= 33.75
Second round, Ann yields	$P1 * 0\% * \$200$	
Second round, both yield	$P1 * 0\% * \$200$	
Anger after Second round	$P1 * 75\% * 20\% * \$0$	

(Note: Chances we go on to third round = $P2 = 50\% * 90\% * 75\% * 80\%$.)

Third round, Bart yields	$P2 * 75\% * \$300$	= 60.75
Third round, Ann yields	$P2 * 0\% * \$200$	
Third round, both yield	$P2 * 0\% * \$200$	
Anger after Third round	$P2 * 25\% * 30\% * \$0$	

(Note: Chances we go to fourth round = $P3 = 50\% * 90\% * 75\% * 80\% * 25\% * 70\%$.)

Third round, Bart yields	$P2 * 100\% * \$300$	= 14.175
Third round, Ann yields	$P2 * 0\% * \$200$	
Third round, both yield	$P2 * 0\% * \$200$	
Anger after Third round	$P2 * 0\% * 40\% * \$0$	

Ann's Expected Payoff = 258.675

... Ann is better off with her strategy than yielding for sure in Round 1 (which gives guaranteed payoff 200)